

## Fourierreihe

### Eulerformeln

$$e^{jx} = \cos(x) + j \sin(x),$$

$$\sin(x) = \frac{e^{jx} - e^{-jx}}{2j}, \quad \cos(x) = \frac{e^{jx} + e^{-jx}}{2}$$

$$T = \frac{2\pi}{\omega} \quad \omega = 2\pi\nu$$

### Fourierreihe von $T$ -periodischen Funktionen

$$f(t) = \frac{a_0}{2} + \sum_{n=1}^{\infty} (a_n \cos(n\omega t) + b_n \sin(n\omega t))$$

$$a_n = \frac{2}{T} \int_0^T f(t) \cos(n\omega t) dt \quad a_0 = \frac{2}{T} \int_0^T f(t) dt$$

$$b_n = \frac{2}{T} \int_0^T f(t) \sin(n\omega t) dt$$

### Komplexe Darstellung

$$f(t) = \sum_{n=-\infty}^{\infty} c_n e^{jn\omega t}, \quad c_n = \frac{1}{T} \int_0^T f(t) e^{-jn\omega t} dt$$

Umrechnung:

$$c_0 = \frac{a_0}{2}, \quad c_n = \frac{1}{2}(a_n - jb_n),$$

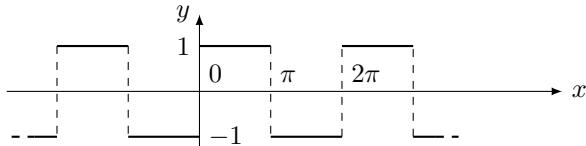
$$c_{-n} = \frac{1}{2}(a_n + jb_n), \quad n = 1, 2, 3, \dots$$

### Satz von Parseval

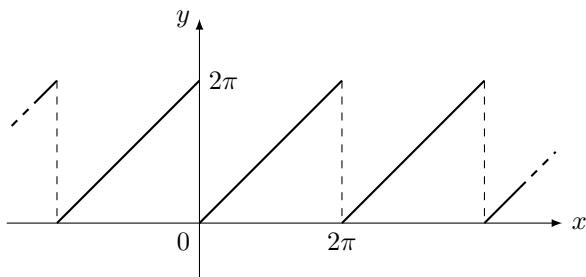
$$\frac{1}{T} \int_0^T f(t)^2 dt = \sum_{n=-\infty}^{\infty} |c_n|^2 = \frac{a_0^2}{4} + \frac{1}{2} \sum_{n=1}^{\infty} (a_n^2 + b_n^2)$$

## Tabellen

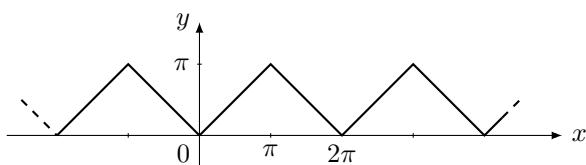
### Wichtige Fourierreihen



$$f(x) = \frac{4}{\pi} \sum_{n \text{ ungl.}} \frac{\sin(nx)}{n}$$



$$f(x) = \pi - 2 \sum_{n=1}^{\infty} \frac{\sin(nx)}{n}$$



$$f(x) = \frac{\pi}{2} - \frac{4}{\pi} \sum_{n \text{ ungl.}} \frac{\cos(nx)}{n^2}$$